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# $hhjj$ production at the LHC

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**Abstract** The search for di-Higgs production at the LHC in order to set limits on the Higgs trilinear coupling and constraints on new physics is one of the main motivations for the LHC high-luminosity phase. Recent experimental analyses suggest that such analyses will only be successful if information from a range of channels is included. We therefore investigate di-Higgs production in association with two hadronic jets and give a detailed discussion of both the gluon- and the weak boson-fusion (WBF) contributions, with a particular emphasis on the phenomenology with modified Higgs trilinear and quartic gauge couplings. We perform a detailed investigation of the full hadronic final state and find that  $hhjj$  production should add sensitivity to a di-Higgs search combination at the HL-LHC with  $3 \text{ ab}^{-1}$ . Since the WBF and GF contributions are sensitive to different sources of physics beyond the Standard Model, we devise search strategies to disentangle and isolate these production modes. While gluon fusion remains non-negligible in WBF-type selections, sizeable new physics contributions to the latter can still be constrained. As an example of the latter point we investigate the sensitivity that can be obtained for a measurement of the quartic Higgs–gauge boson couplings.

## 1 Introduction

After the Higgs boson discovery in 2012 [1, 2] and subsequent analyses of its properties [3, 4], evidence for physics beyond the Standard Model (BSM) remains elusive. Although consistency with SM Higgs properties is expected in many BSM

scenarios, current measurements do not fully constrain the Higgs sector. One coupling which is currently unconstrained and has recently been subject of much interest is the Higgs self-interaction  $\sim \eta$ , which is responsible for the spontaneous breaking of electroweak gauge symmetry in the SM via the potential

$$V(H^\dagger H) = \mu^2 H^\dagger H + \eta (H^\dagger H)^2, \quad (1)$$

with  $\mu^2 < 0$ , where  $H = (0, v + h)^T / \sqrt{2}$  in unitary gauge. The Higgs self-coupling manifests itself primarily in destructive interference in gluon-fusion-induced di-Higgs production [5–11] through feeding into the trilinear Higgs interaction with strength  $\lambda_{\text{SM}} = m_h \sqrt{\eta/2} = gm_h^2/(4m_W)$  in the SM. The latter relation can be altered in BSM scenarios, e.g. the SM coupling pattern can be distorted by the presence of a dimension six operator  $\sim (H^\dagger H)^3$ , and di-Higgs production is the only channel with direct sensitivity to this interaction [12, 13]. A modification solely of the Higgs trilinear coupling, which is typically invoked in di-Higgs feasibility studies, is predicted in models of  $\mu^2$ -less electroweak symmetry breaking, e.g. [14].

After the Higgs discovery, analyses of the di-Higgs final state at the high-luminosity LHC and beyond have experienced a renaissance, and di-Higgs final states such as the  $b\bar{b}\gamma\gamma$  [12, 13, 15–17],  $b\bar{b}\tau^+\tau^-$  [18–20],  $b\bar{b}W^+W^-$  [18, 19, 21] and  $b\bar{b}b\bar{b}$  [18, 19, 22] channels have been studied phenomenologically, often relying on boosted jet substructure techniques [23] (see also an investigation [24] of rare decay channels relevant for a 100 TeV collider). Recent analyses by ATLAS and CMS [25, 26] have highlighted the complexity of these analyses and the necessity to explore different production mechanisms to formulate constraints on the Higgs self-interactions in the future. This program has already been initiated by feasibility analyses of the  $hhj$ ,  $hhjj$  and  $t\bar{t}hh$  production modes in Refs. [17, 19, 27–29].

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Di-Higgs production in association with two jets is a particularly important channel in this regard since this final state receives contributions from the weak boson-fusion (WBF) production mode. The phenomenological appeal of the WBF mode is twofold. Firstly, the WBF component of  $pp \rightarrow hhjj$  is sensitive to modifications of the gauge–Higgs sector [27, 30], which can lead to large cross-section enhancements. Secondly, the QCD uncertainties for the WBF topologies are known and under theoretical control [31, 32], such that a search for BSM electroweak-induced deviations is not hampered by QCD systematics. This situation is very different from QCD-induced production [33–36], and can be attributed to the particular phenomenology of WBF-like processes [37–40].

However, an additional source of uncertainty that was neglected until recently [27] is the correct inclusion of the gluon-fusion contribution to  $pp \rightarrow hhjj$  analyses. In contrast to single Higgs phenomenology, the correct inclusion of massive fermion thresholds is crucial to a reliable prediction of QCD-induced  $pp \rightarrow hhjj$  [19].

Given that the cross sections in WBF  $hhjj$  production are very suppressed compared to WBF  $hjj$  production (the WBF  $hhjj$  cross section is  $\sim 750$  times smaller), we have to rely on the dominant hadronic Higgs decay modes to be able to observe this final state. This rules out one of the most crucial single Higgs WBF selection tools—the central jet veto [41]. The observation of WBF-induced  $pp \rightarrow hhjj$  production is further hampered by the top threshold in the QCD-mediated process. Since the top threshold sets the scale of the di-Higgs subsystem, an analysis that tries to retain as many low  $p_T$  Higgs bosons as possible leads to a QCD contribution that dominates over the WBF component when minimal WBF-like cut requirements are imposed [27].

In this paper we extend the discussion of Ref. [27] in a number of directions. We first perform a detailed comparison of EFT-approaches to QCD-mediated  $pp \rightarrow hhjj$  against a calculation keeping the full mass dependencies of top and bottom quarks in Sect. 2. We compare the QCD-induced  $pp \rightarrow hhjj$  phenomenology to the WBF signature in Sect. 3 before we discuss general approaches to isolate the signal from the dominant top backgrounds in a hadron-level analysis in Sect. 4. This sets the stage for a discussion of the prospects to isolate the WBF and GF components in Sects. 4.1 and 4.2, followed by a study on constraining  $VVhh$  couplings using the WBF induced signal in Sect. 4.3. We focus on collisions with 14 TeV throughout.

## 2 The gluon-fusion contribution

### 2.1 Finite top mass effects

It is well known that effective field theory approximations in the  $m_t \rightarrow \infty$  limit cannot be invoked to study di-Higgs

final states at colliders in a reliable way due to the effects of top-quark threshold [10, 42]. Further, the breakdown of the  $m_t \rightarrow \infty$  approximation is worsened in the presence of additional jet emission [19, 43]. Finite  $m_t$  effects must therefore be considered for all QCD di-Higgs production channels, which will be required to set the best limits on the Higgs self-coupling or formulate a realistic estimate of the GF contribution in a WBF-like selection.

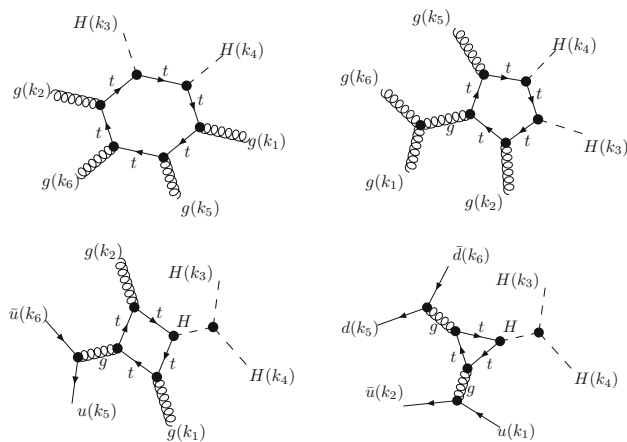
The computational challenges in QCD-mediated  $hhjj$  production are significant, with the gluon-fusion channels particularly time consuming even when using state-of-the-art techniques. The standard method of simulating a differential cross section from unweighted events is not feasible in this case, and we instead use a reweighting technique that is exploited in higher order calculations and experimental analyses (see e.g. [44]).

We generate GF  $hhjj$  events by implementing the relevant higher dimensional operators in the  $m_t \rightarrow \infty$  limit obtained by expanding the low-energy effective theory [45–47]

$$\mathcal{L}_{\text{eff}} = -\frac{1}{4} \frac{\alpha_S}{3\pi} G_{\mu\nu}^a G^{a\mu\nu} \log(1 + h/v) \quad (2)$$

in MADEVENT v5.1 [48] using the FEYNRULES/UFO [49] framework.<sup>1</sup> This allows us to sample a weighted set of events that we subsequently feed into our analysis solely depending on their final state kinematics. If an event passes the selection requirements of a certain search region, we correct for the full mass dependence using a reweighting library based on GOSAM package [50, 51] at this stage. The reweighting employs exactly the same matrix elements used for the event generation and the trilinear coupling is steered through a modification of the GOSAM matrix element, i.e. variations of the trilinear coupling are part of the reweighting. A selection of Feynman diagrams which contribute to the gluon-fusion signal are illustrated in Fig. 1. The GOSAM code used for the reweighting is based on a Feynman diagrammatic approach using QGRAF [52] and FORM [53, 54] for the diagram generation, and on SPINNEY [55], HAGGIES [56] and FORM for writing an optimised fortran output. The reduction of the one-loop amplitudes was done using SAMURAI [57], which uses a  $d$ -dimensional integrand-level decomposition based on unitarity methods [58–62]. The remaining scalar integrals have been evaluated using ONELOOP [63]. Alternative reduction techniques can be used employing NINJA [64–67] or GOLEM95 [68–70]. To validate the reweighting procedure we regenerated the code that has been used in [27] with the improvements that became available within GOSAM 2.0, in particular improvements in code optimisation and in the

<sup>1</sup> The effective theory implementation can be modified in the sense that only one effective vertex insertion is allowed. This gives only a mild  $\sim 10\%$  effect in the tail of the distribution and is not relevant for an order one EFT/full theory rescaling, see below.



**Fig. 1** Sample Feynman diagrams contributing to  $pp \rightarrow hhjj$  via gluon fusion

reduction of the amplitudes. For the reduction we used NINJA, which employs an improved reduction algorithm based on a Laurent expansion of the integrand. This leads to substantial improvements in both speed and numerical stability compared to the previous version. We combined the code with a phase space integration provided by MADEVENT [71]. Further substantial speed-up has been obtained by Monte Carlo sampling over the helicities rather than performing the helicity sum. This enabled us to perform a full phase space integration and we found full agreement within the statistical uncertainties between the result obtained from reweighting and the result from the full phase space integration.

## 2.2 Phenomenology of QCD-mediated $hhjj$ production

Top thresholds are particularly prominent in the di-Higgs invariant mass distribution, which is thus well suited to benchmark the relation of the finite  $m_t$  limit to the effective theory of Eq. 2. Other observables constructed from the six particle final state are also relevant when performing a targeted phenomenological analysis, and we discuss both these and the phase space dependent parton-level reweighting in detail in the following.

In Figs. 2, 3 and 4 we show a selection of  $hhjj$  final state observables for inclusive cuts  $p_{T,j} > 20$  GeV and  $|\eta_j| < 5$ ; no cuts on Higgs bosons are imposed. We label Higgs bosons and jets according to their hardness, i.e.  $p_{T,h1} > p_{T,h2}$  and  $p_{T,j1} > p_{T,j2}$ . The cross sections are given in Table 1. The inclusive gluon-fusion cross section is about 2.5 times larger than the WBF cross section approximately independent of the value of the Higgs trilinear coupling.

As previously established in [10, 19, 27] the di-Higgs system is badly modelled by the effective theory which under- and overshoots the full theory cross section at low and high momenta respectively. For  $pp \rightarrow hhjj$  this is a qualita-

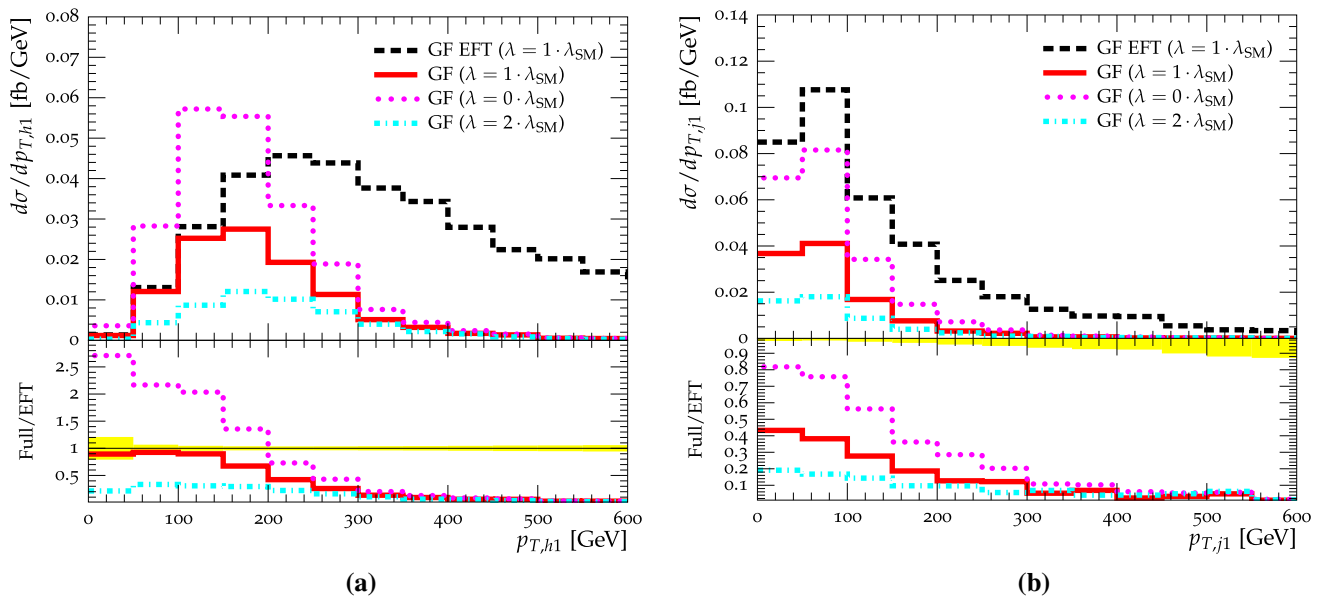
tively similar behaviour compared the  $pp \rightarrow hh(j)$  production: The  $m_{hh}$  distribution is the crucial observable which parametrises the finite top quark mass effects. The EFT describes the low maximum transverse Higgs momenta  $p_{T,h1}$  reasonably well, as shown in Fig. 2a. The jet emission on the other hand integrates over a considerable range of  $m_{hh}$ , and the ratio of full theory vs effective theory smaller than one for the finite  $m_t$  limit produces a smaller integrated cross section than the  $m_t \rightarrow \infty$  limit for the jet kinematics.

Considering just the dijet system in Fig. 3, we observe that the jet kinematics is not severely impacted by the reweighting procedure upon marginalising over the di-Higgs kinematics. The phase space dependence of the dijet invariant mass Fig. 3a is relatively mild aside from the total rescaling of the inclusive cross sections, and the ratio for the pseudo-rapidity distribution of the jets is nearly flat; see Fig. 3b. This is also true for the azimuthal angle difference  $\Delta\phi_{jj}$ . The angular distributions of the leading members of the jet-Higgs system are relatively mildly impacted by the reweighting too Fig. 4b. This agrees with the  $m_{hh}$  being the observable most sensitive to the top threshold [as in  $pp \rightarrow hh(j)$ ], and is also supported by the larger impact of the reweighting of  $m_{hh}$  in Fig. 4a. A reweighting based on  $m_{hh}$  to correct for finite top mass effects suggests itself for future analyses as a time-saving approach with reasonable accuracy.

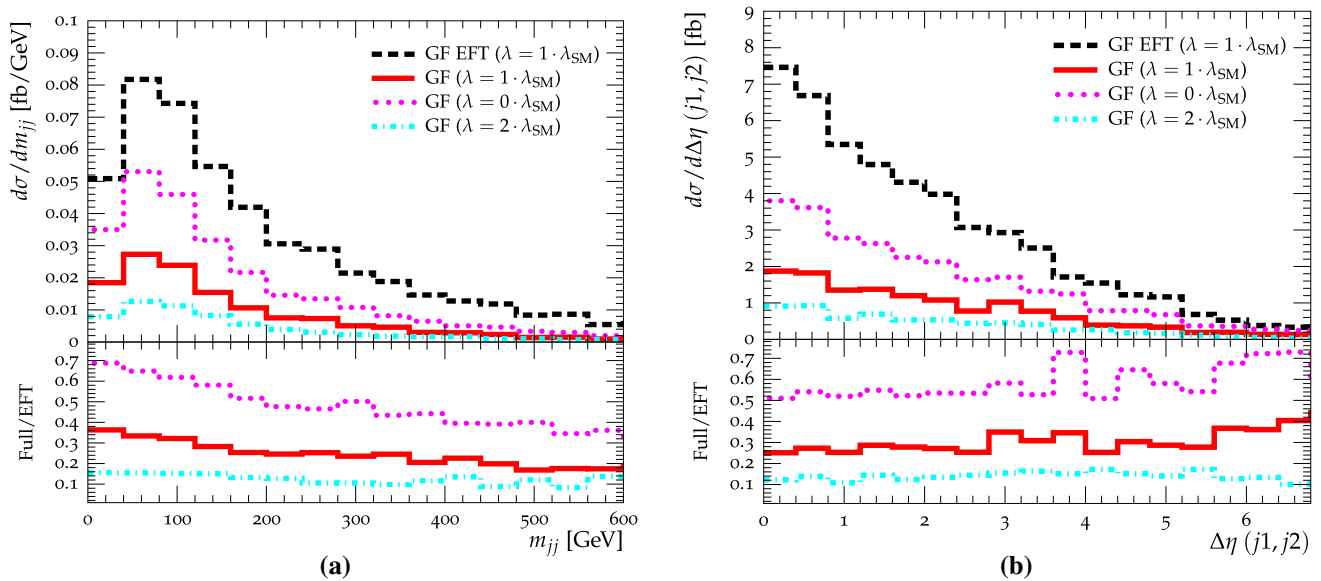
## 3 The weak boson-fusion contribution

The WBF contribution to  $pp \rightarrow hhjj$  has received considerable attention recently and precise higher-order QCD corrections have been provided in [31, 32, 40]. Due to the sensitivity of the WBF contribution to both the trilinear coupling and the quartic  $VVhh$  ( $V = W, Z, \gamma$ ), as shown in the Feynman diagrams in Fig. 5, WBF to two Higgs bosons can, in principle, provide complementary information as regards BSM physics, which remains uncaptured in  $pp \rightarrow hh(j)$  and  $pp \rightarrow t\bar{t}hh$  [30].

We generate WBF samples with varying  $\lambda$  using MADEVENT v4 [72] and normalise the cross section to NLO accuracy [31]. The WBF  $hhjj$  contribution shares the QCD properties of WBF  $hjj$  production [37–39] which means it shares the distinctive  $\Delta\eta(j1, j2)$  distribution shown in Fig. 6a: to produce the heavy di-Higgs pair we probe the initial state partons at large momentum fractions. This together with a colour-neutral  $t$ -channel exchange of the electroweak bosons [73] (see also [74, 75]) leads to energetic back-to-back jet configurations at large rapidity separation and moderate transverse momenta with a centrally produced Higgs pair. The production of an additional Higgs boson in comparison to single Higgs production via WBF leads to a cross-section reduction by three orders of magnitude (see Table 1) in the SM. Such a small inclusive production cross section high-



**Fig. 2** Maximum Higgs and jet transverse momenta for gluon-fusion-induced  $hhjj$  production, including the ratio of full theory to the effective theory calculation for three different values of the Higgs trilinear coupling  $\lambda$



**Fig. 3** Invariant mass and pseudo-rapidity distributions of the jet system in QCD-mediated  $hhjj$  production. We show the effective theory and full theory results for three values of the trilinear Higgs coupling, applying only generator-level cuts of  $p_{T,j} \geq 20$  GeV and  $|\eta_j| < 5$

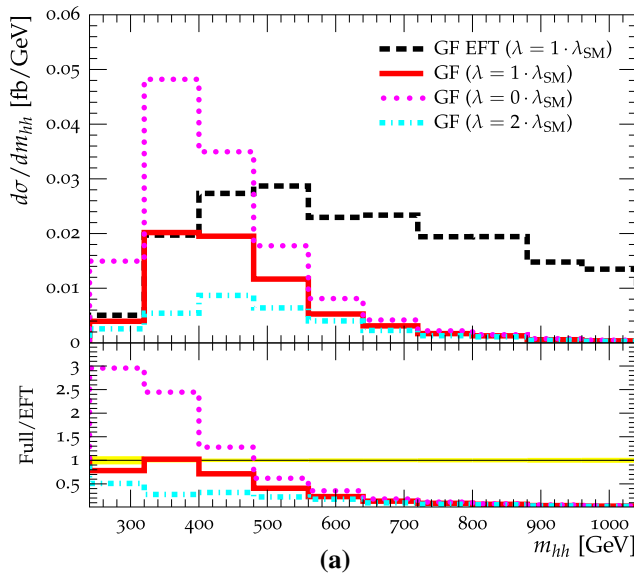
lights the necessity of considering dominant Higgs decay channels such as  $h \rightarrow b\bar{b}$  and  $h \rightarrow \tau^+\tau^-$  and the non-availability of central jet vetos [41] as a means to control the background and GF contribution in a targeted analysis as a consequence.

The gluon-fusion contribution is bigger by a factor of 2.5 than the WBF component of  $hhjj$  production, however, with increasing invariant di-Higgs mass the WBF contribution is enhanced relative to GF production as a consequence of the suppression above the  $2m_t$  threshold, as shown in Fig. 6b.

Since we cannot rely on vetoing hadronic activity in the central part of the detector, a potential discrimination of GF from WBF needs to be built on the following strategy, which we will investigate in Sect. 4:

- To isolate the di-Higgs (WBF+GF) signal we can exploit the relative hardness of the di-Higgs pair which peaks around  $\sim 2m_t$ . Such hard events are less likely to be produced by (ir)reducible backgrounds.
- Focussing on large  $m_{hh}$  we can enhance WBF over GF by stringent cuts on the jet rapidity separation. This will also





**Fig. 4** Invariant mass and pseudo-rapidity distributions of the leading jet and di-Higgs system in QCD-mediated  $hhjj$  production. We show the effective theory and full theory results for three values of the trilinear

**Table 1** Cross-section normalisations for the GF and WBF samples at 14 TeV, for details see text. The WBF normalisation follows from [31] and includes higher order QCD effects

$\lambda$	$0 \cdot \lambda_{\text{SM}}$ (fb)	$1 \cdot \lambda_{\text{SM}}$ (fb)	$2 \cdot \lambda_{\text{SM}}$ (fb)
GF	10.73	5.502	2.669
WBF	4.141	2.010	0.9648

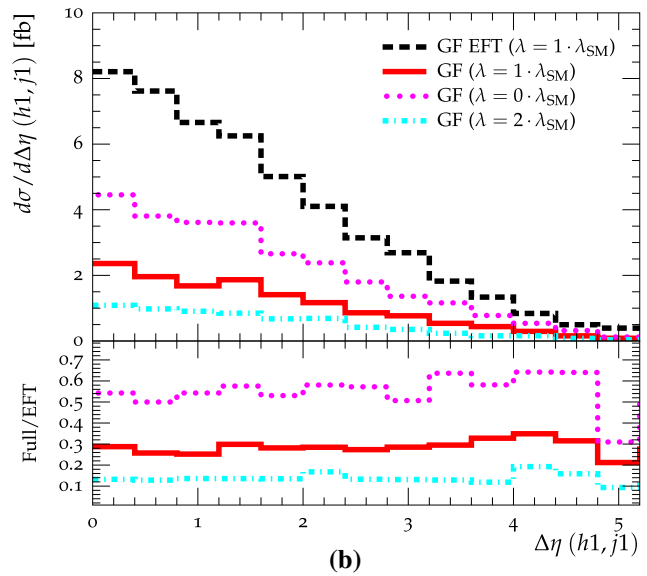
imply a significant decrease of QCD-dominated backgrounds.

- By explicitly allowing central jet activity, we can exploit the colour correlation differences in WBF vs. GF to further purify our selection. Since colour flow is tantamount to energy flow in the detector, event shapes are particularly well-suited observables for unravelling the colour correlations in the final state once the reconstructed di-Higgs pair has been removed.<sup>2</sup> This strategy was first proposed for single Higgs analyses in [78] (see also [79]).

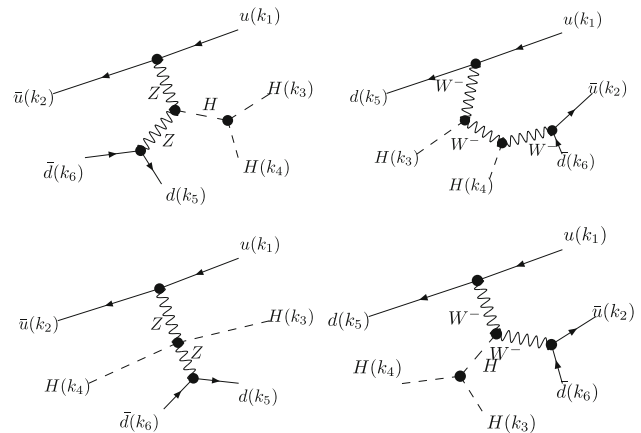
#### 4 Taming the background

For our hadron-level analysis we shower our signal samples with HERWIG++ [80] and generate backgrounds as follows:  $t\bar{t}jj$ ,  $t\bar{t}h$ ,  $Zhjj$  and  $ZZjj$  with SHERPA [81] and  $ZWWjj$  with MADEVENT v5. We find the dominant backgrounds to be  $t\bar{t}jj$  and  $t\bar{t}h$  production, for which next-to-leading order results are available [82–93] and we use inclusive  $K$  factors

<sup>2</sup> A detailed discussion of event shapes at hadron colliders can be found in [76, 77].



Higgs coupling, applying only generator-level cuts of  $p_{T,j} \geq 20$  GeV and  $|\eta_j| < 5$



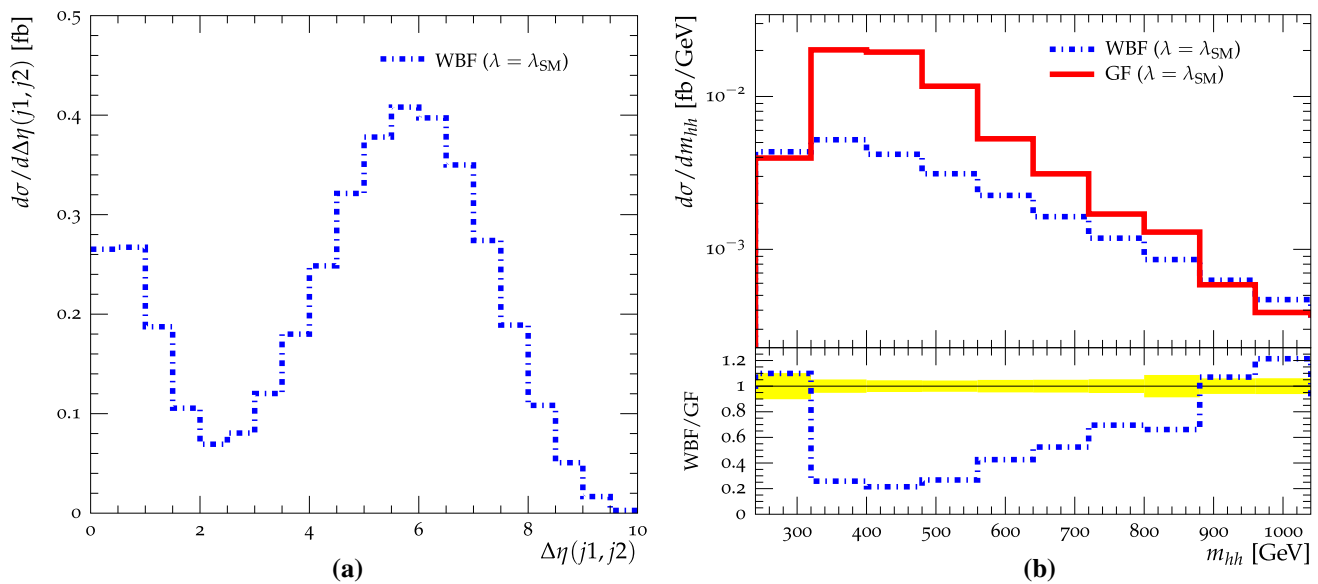
**Fig. 5** Sample Feynman diagrams contributing to  $pp \rightarrow hhjj$  in weak boson fusion

$K_{t\bar{t}jj} \simeq 1$  and  $K_{t\bar{t}h} \simeq 1.5$  to estimate the higher order contributions to these backgrounds. Higgs branching ratios are set to the values agreed upon by the Higgs Cross Section Working Group [94].

We begin the hadron-level analysis implemented in Rivet [95] by recreating a base selections similar to [27]<sup>3</sup>:

- (1) We require two tau leptons using a two tau-trigger based on staggered transverse momentum selection cuts  $p_T \geq 29, 20$  GeV in  $|\eta_\tau| < 2.5$  and assume a flat tau tagging efficiency of 70 % with no fakes. Jets are constructed by

<sup>3</sup> Our analysis has been validated with two independent implementations.



**Fig. 6** The  $\Delta\eta(j1, j2)$  distribution of the WBF contribution at parton level (a) and the  $m_{hh}$  distribution of the WBF and gluon-fusion contributions compared with correct cross-section normalisation (b), both satisfying generator-level cuts of  $p_{T,j} \geq 20$  GeV and  $|\eta_j| < 5$

clustering  $R = 0.4$  anti- $k_T$  jets using FASTJET [96] with  $p_{T,j} \geq 25$  GeV and  $|\eta_j| \leq 4.5$ .

- (2) The two leading jets are  $b$ -tagged with an acceptance of 70 % and fake rate of 1 % [97] in the central part of the detector  $|\eta_j| < 2.5$ . We remove events if either of the two leading jets overlaps with a tau. Any additional jets which do not overlap with a tau are considered as potential “tagging jets”, of which we require at least two.<sup>4</sup>
- (3) As a final step of this base selection we require the  $b$  jet and tau pairs to reproduce the Higgs mass of 125 GeV within  $\pm 15$  and  $\pm 25$  GeV, respectively.<sup>5</sup>

The signal and background cross sections after these cuts are presented in the base selection column of Table 2. We find that the background contribution of  $t\bar{t}jj$  dominates with  $t\bar{t}h$  also providing a larger-than-signal background resulting in  $S/B \sim 1/300$ , making a study based only on these selections extremely challenging. Since we only have  $\sim 40$  expected gluon fusion and  $\sim 10$  expected WBF events at  $3 \text{ ab}^{-1}$  luminosity, additional selections must also be careful to retain enough signal cross section to allow statistically meaningful statements to be made with a finite amount of data.

<sup>4</sup> It was argued recently [98] that single jet tagging [99] could provide an alternative at high luminosity for single Higgs production at lost WBF/GF purity.

<sup>5</sup> A high mass resolution is a crucial cornerstone of any successful di-Higgs analysis to assure a minimum pollution of Z boson decay backgrounds [20].

Shape comparisons for the rapidity and di-Higgs invariant mass distributions as motivated in the previous section are shown in Fig. 7. Indeed, as expected, cutting on the angular distance of the jets will serve to purify towards a WBF-only selection at a reduced background rate. The dominant backgrounds are unlikely to produce a large invariant mass  $m_{hh}$ . However, the WBF contribution, due to the lack of the  $2m_t$  threshold peaks at a considerably lower invariant mass, leading to significant decrease of the WBF contribution for a reasonably strong cut on  $m_{hh}$ , which is required to observe the  $hhjj$  signal at the given low signal yield, even at  $3 \text{ ab}^{-1}$  luminosity.

#### 4.1 Prospects to isolate gluon fusion

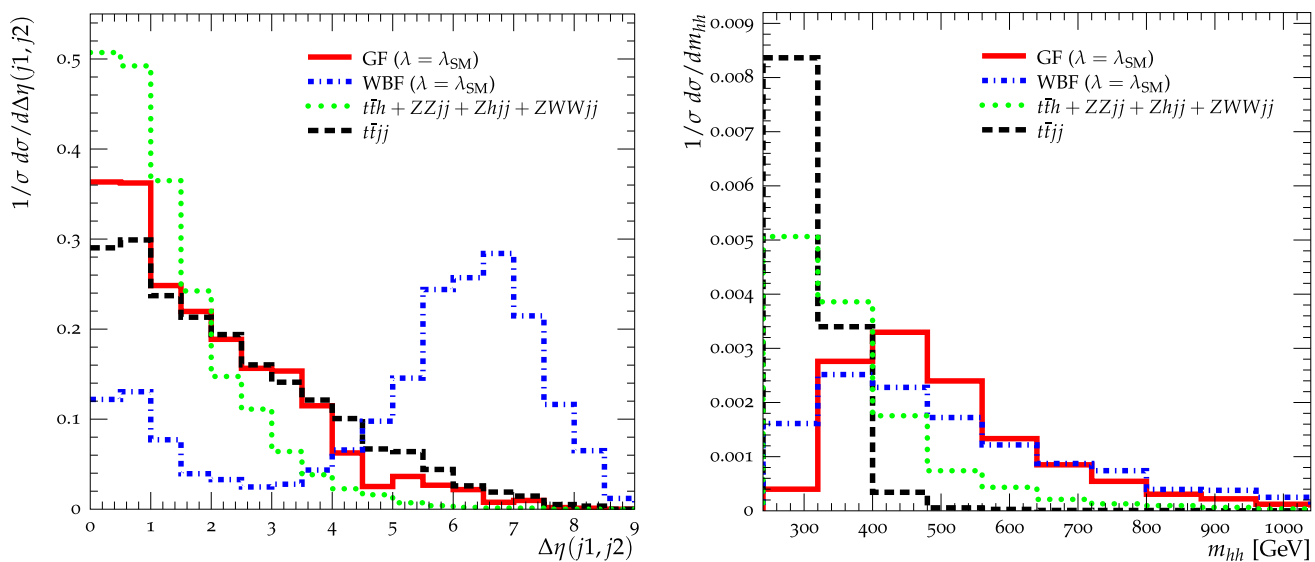
We can extend the analysis outlined in Sect. 4 with the aim to purify the selection towards the GF component.<sup>6</sup> We make use of the hard Higgs candidates to greatly reduce the backgrounds by requiring  $m_{hh} \geq 500$  GeV and additionally require  $\Delta\eta(j1, j2) \leq 5$  to minimise the WBF contribution. The signal and background cross sections after these cuts are applied are presented in the ‘GF selection’ column of Table 2.

The total background is reduced by a factor of  $\sim 100$ , while the gluon-fusion contribution only is reduced by a factor of  $\sim 2.5$  which allows for an encouraging  $S/\sqrt{B} \sim 1.7$  with  $3 \text{ ab}^{-1}$  of data. The WBF contribution is also suppressed compared to GF which allows for a clean probe of the physics accessible in the gluon-fusion contribution.

<sup>6</sup> Following the analysis of [100], we can expect negligible interference between WBF and GF and which allows us to make this distinction.

**Table 2** Cross sections for the two sources of signal and backgrounds, after the various selections described in the text are applied, together with various measures of significance in the bottom four rows

Cut setup	Base selection (fb)	GF selection (fb)	WBF selection (fb)	Normalisation <sup>a</sup> (fb)
GF ( $\lambda = 1 \cdot \lambda_{\text{SM}}$ )	$1.396 \times 10^{-2}$	$5.722 \times 10^{-3}$	$5.378 \times 10^{-4}$	$4.013 \times 10^{-1}$
GF ( $\lambda = 0 \cdot \lambda_{\text{SM}}$ )	$2.562 \times 10^{-2}$	$8.122 \times 10^{-3}$	$8.767 \times 10^{-4}$	$7.831 \times 10^{-1}$
GF ( $\lambda = 2 \cdot \lambda_{\text{SM}}$ )	$7.167 \times 10^{-3}$	$3.906 \times 10^{-3}$	$3.034 \times 10^{-4}$	$1.947 \times 10^{-1}$
WBF ( $\lambda = 1 \cdot \lambda_{\text{SM}}$ )	$3.292 \times 10^{-3}$	$4.999 \times 10^{-4}$	$1.485 \times 10^{-3}$	$1.466 \times 10^{-1}$
WBF ( $\lambda = 0 \cdot \lambda_{\text{SM}}$ )	$7.706 \times 10^{-3}$	$7.154 \times 10^{-4}$	$2.820 \times 10^{-3}$	$3.020 \times 10^{-1}$
WBF ( $\lambda = 2 \cdot \lambda_{\text{SM}}$ )	$1.103 \times 10^{-3}$	$1.815 \times 10^{-4}$	$3.912 \times 10^{-4}$	$7.037 \times 10^{-2}$
$t\bar{t}jj$	5.712	$3.390 \times 10^{-2}$	$1.801 \times 10^{-2}$	$1.0130 \times 10^4$
$t\bar{t}h$	$6.229 \times 10^{-2}$	$7.047 \times 10^{-3}$	$5.658 \times 10^{-5}$	$3.862 \times 10^1$
$Zhjj$	$5.118 \times 10^{-3}$	$1.278 \times 10^{-3}$	$1.026 \times 10^{-4}$	$4.737 \times 10^1$
$ZZjj$	$1.171 \times 10^{-3}$	$6.659 \times 10^{-5}$	$7.639 \times 10^{-7}$	$2.257 \times 10^2$
$ZWWjj$	$1.888 \times 10^{-5}$	$5.461 \times 10^{-6}$	$2.039 \times 10^{-7}$	$5.368 \times 10^{-1}$
Total background	5.781	$4.230 \times 10^{-2}$	$1.817 \times 10^{-2}$	–
$S/B$ ( $\lambda = 1 \cdot \lambda_{\text{SM}}$ )	1/335.1	1/6.799	1/8.983	
$S/B$ GF <sup>b</sup> ( $\lambda = 1 \cdot \lambda_{\text{SM}}$ )	1/414.3	1/7.480	1/36.55	
$S/B$ WBF <sup>b</sup> ( $\lambda = 1 \cdot \lambda_{\text{SM}}$ )	1/1760	1/96.06	1/12.60	
$S/\sqrt{B}$ ( $3 \text{ ab}^{-1}$ , $\lambda = 1 \cdot \lambda_{\text{SM}}$ )	0.3930	1.657	0.8219	

<sup>a</sup> Branchings included in normalisation<sup>b</sup> Considering only this as signal**Fig. 7** Shape comparison of  $\Delta\eta(j1, j2)$  and  $m_{hh}$  distributions for our two sources of signal (GF and WBF), the dominant background  $t\bar{t}jj$  and the rest of the backgrounds (stacked scaled by relative cross sections), after the base selection of Sect. 4 has been applied

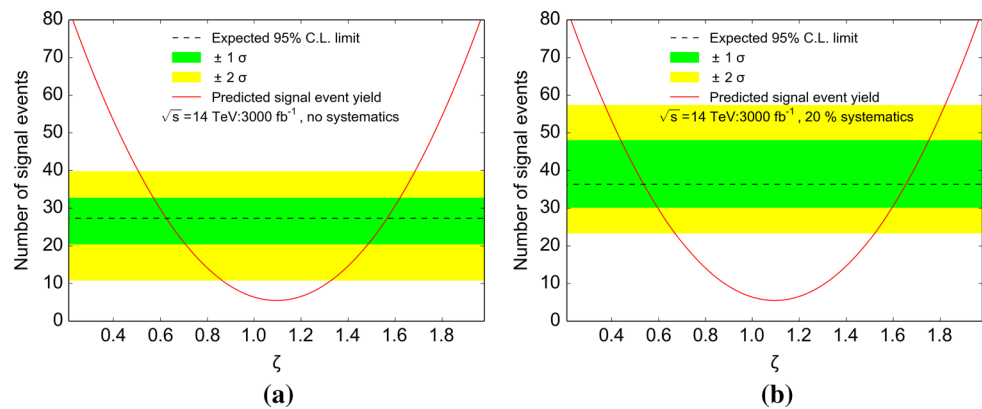
#### 4.2 Prospects to isolate weak boson fusion

Similarly we can extend the analysis towards isolating the WBF component. Since it has slightly softer Higgs candidates we require  $m_{hh} \geq 400$  GeV and  $\Delta\eta(j1, j2) \geq 5$  to reduce both the gluon-fusion and the background contributions. The signal and background cross sections after these cuts are applied are presented in the ‘WBF selection’ column of Table 2.

The total background is reduced by a factor of  $\sim 300$  while three times more of the WBF contribution is retained compared to the GF selection, resulting in  $S/\sqrt{B} \sim 0.8$  with  $3 \text{ ab}^{-1}$  of data due to the large reduction in the gluon-fusion contribution. However, even so the WBF selection is composed of one-to-three parts GF to WBF, which means measurements of physics that only enters the WBF contribution will need to take this gluon-fusion ‘pollution’ into account.



**Fig. 8** Expected limits on the gauge–Higgs quartic couplings  $\zeta = g_{VVhh}/g_{VVhh}^{\text{SM}}$  under the assumption of no systematic uncertainties (a) and 20 % systematic uncertainties (b)



#### 4.3 Constraining the quartic $VVhh$ contribution

As mentioned in Sect. 3 there is a contribution from quartic  $VVhh$  vertices to the WBF-induced signal, and modifications of the corresponding  $g_{VVhh}$  couplings away from their SM values using the Higgs Cross Section Working Group  $\kappa$  framework [94] will greatly enhance the signal cross section. This allows us to constrain  $\zeta$  defined by  $g_{VVhh} = \zeta \times g_{VVhh}^{\text{SM}}$ . To achieve this we have generated events with varying  $\zeta$  using MADEVENT v5 and applied the WBF selections described in Sect. 4.2 to estimate the enhancement of the signal, which is compared to expected cross-section limits on the signal with  $3 \text{ ab}^{-1}$  of data in the WBF selection under the assumptions of no systematic uncertainties and 20 % total systematic uncertainties for comparison. The results are presented in Fig. 8. We find that in the more realistic scenario of 20 % systematic uncertainties the expected constraint on the  $g_{VVhh}$  couplings is  $0.55 < \zeta < 1.65$  at 95 % confidence level. A measurement of  $pp \rightarrow hhjj$  is therefore crucial to constrain new physics which enters predominantly through enhancements to  $g_{VVhh}$ .

#### 4.4 Event shapes of the tagging jets system

The analysis strategies outlined so far have mainly relied on exploiting correlations in the di-Higgs system, with only  $\Delta\eta(j1, j2)$  carrying information about the tagging jets. Following similar applications in the context of single Higgs production [78], we investigate a range of event shapes in the tagging jets system in the following, which could offer additional discriminating power through capturing colour correlations in the different signal contributions beyond angular dependencies. More specifically, we will focus on  $N$ -jettiness [101, 102] and thrust major (defined below) which provided the best results.

We calculate  $N$ -jettiness by minimising

$$\tau_N = C \sum_k p_{T,k} \min(\Delta R_{k,1}, \dots, \Delta R_{k,N}) \quad (3)$$

where  $C$  is a normalisation which cancels when taking the ratio of two  $\tau$ s, the sum is taken over all visible momenta which do not belong to one of the identified Higgs candidates within  $|\eta| < 5$ , and  $\Delta R_{k,n}$  is the distance in the  $\eta$ – $\phi$  plane between the  $k$ th momentum and the  $n$ th reference vector.  $\tau_{3/2}$  is then explicitly given by  $\tau_3/\tau_2$ .

Thrust major is defined by

$$T_{\text{maj}} = \max_{\mathbf{n} \cdot \mathbf{n}_T = 0} \frac{\sum_k |\mathbf{p}_k \cdot \mathbf{n}|}{\sum_k |\mathbf{p}_k|} \quad (4a)$$

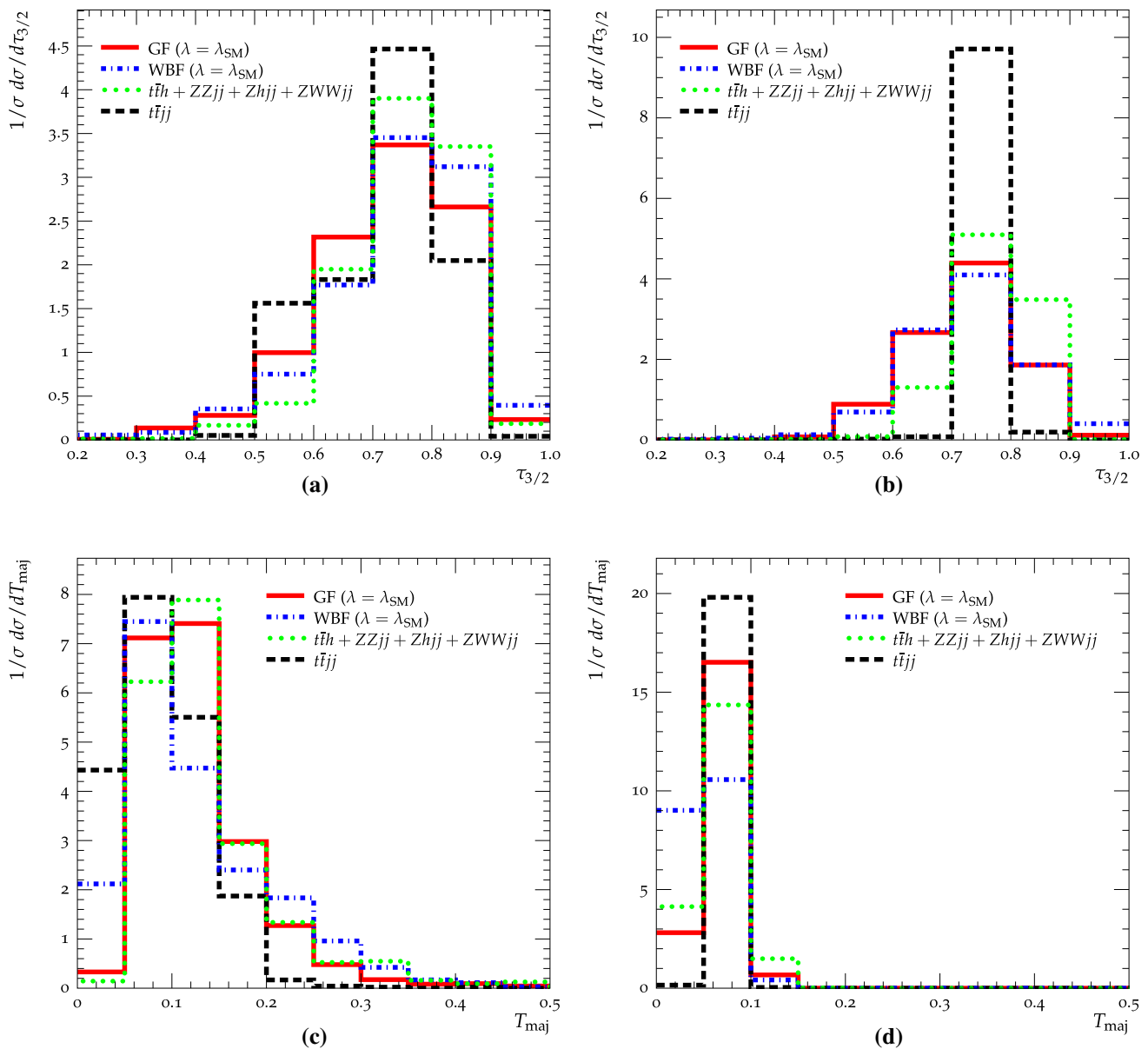
where  $\mathbf{n}_T$  is the normalised thrust vector

$$\mathbf{n}_T = \max_{\mathbf{n}} \frac{\sum_k |\mathbf{p}_k \cdot \mathbf{n}|}{\sum_k |\mathbf{p}_k|}. \quad (4b)$$

Again the sums run over all visible momenta which do not belong to one of the identified Higgs candidates within  $|\eta| < 5$ .

We find  $\tau_{3/2}$  and  $T_{\text{maj}}$  show promise for improving the WBF selection, but the signal cross section is already too low for us to be able to make meaningful use of this insight. The  $\tau_{3/2}$  and  $T_{\text{maj}}$  distributions after the GF and WBF selections have been applied are presented in Fig. 9. Cutting, e.g., on  $T_{\text{maj}} < 0.05$ , the gluon-fusion contribution is reduced by 80 %, while the WBF contribution is reduced by only 55 % amounting to a total of 2 expected WBF and 0.3 expected GF events, with backgrounds very strongly suppressed. This means that WBF can in principle be observed at a small rate that can be used to set constraints on new physics in an almost GF-free selection with greatly reduced backgrounds.

The event shape distributions can also be used to greatly reduce the background in the GF selection, Fig. 9c. It should be noted that these improvements of GF vs. WBF vs. background ultimately depend on underlying event and pile up conditions and have to be taken with a grain of salt at this stage early in run 2. However, the clear separation that can be achieved with these observables indicate that an analysis employing MVA techniques could, at least in theory, significantly improve the results presented here. These techniques



**Fig. 9** Shape comparisons of  $N$ -jettiness and thrust calculated in the major direction after the gluon-fusion selection of Sect. 4.1 (a, c) and WBF selection of Sect. 4.2 (b, d) have been applied

may also prove useful at a 100 TeV collider where the di-Higgs production cross section is substantially higher [17].

## 5 Summary and conclusions

After discovering single Higgs production at the Large Hadron Collider, new analysis strategies need to be explored to further constrain the presence of new physics BSM. Higgs pair production is pivotal in this regard as constraints from multi-Higgs production contain complementary information, in particular with respect to the Higgs boson's self-

interaction. Cross sections for di-Higgs production are generically small at the LHC, which highlights the necessity to explore other viable channels than  $pp \rightarrow hh$  to enhance sensitivity in a combined fit at high luminosity. To this end, we have investigated  $pp \rightarrow hhjj$  production in detail in this paper. Keeping the full top and bottom mass dependencies, we find sensitivity of  $pp \rightarrow hhjj$  searches at the LHC for production in the SM and beyond. The gluon-fusion contribution remains important at high invariant di-Higgs masses where the dominant backgrounds can be suppressed to facilitate a reasonable signal vs background discrimination. Unfortunately, the gluon-fusion contribution remains

large even for selections that enhance the WBF fraction of  $pp \rightarrow hhjj$  events. This “pollution” is important when such selections are employed to set constraints on new physics effects that enter in the WBF contribution exclusively. Large new physics effects in the WBF contribution can still be constrained, which we have illustrated through an investigation of the constraints that can be set on deviations of the quartic  $VVhh$  couplings from their SM values with the HL-LHC, demonstrating that a measurement of  $pp \rightarrow hhjj$  will provide a powerful probe of these. Employing observables which are intrinsically sensitive to the different colour correlation of WBF compared to GF, the discrimination between GF, WBF, and background can be further improved. However, the signal cross section is typically already too small to use such a strategy to constrain the presence of new physics if those effects are only a small deviation around the SM. If new physics effects are sizable, such an approach will remain a well-adapted strategy to minimise GF towards a pure WBF selection.

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